

The Christoffel symbols, $\left\{ \begin{matrix} i \\ \alpha\beta \end{matrix} \right\}$, are obtained from the definitions shown in the next two equations, along with equations Eq 2 and Eq 5. The coefficients, h^{ki} are obtained by inverting the matrix with elements defined by Eq 5. The results are shown below, and the unknown function symbols, y_0 and y_1 , have replaced, respectively $x_0 = r$, and $x_1 = \theta$.

$$\text{Eq 16:} \quad \left\{ \begin{matrix} i \\ \alpha\beta \end{matrix} \right\} \equiv h^{ik} [\alpha\beta, k] = h^{i0} [\alpha\beta, 0] + h^{i1} [\alpha\beta, 1] + h^{i2} [\alpha\beta, 2]$$

$$\text{Eq 17:} \quad [\alpha\beta, k] \equiv \frac{1}{2} \left(\frac{\partial h_{\alpha k}}{\partial x^\beta} + \frac{\partial h_{\beta k}}{\partial x^\alpha} - \frac{\partial h_{\alpha\beta}}{\partial x^k} \right)$$

Let the function F_{cs} be defined by

$$\text{Eq 18:} \quad F(E, k, r) \equiv \frac{\frac{Er}{k} + \frac{1}{2}}{\frac{Er}{k} + 1} = \frac{\frac{Ey_0}{k} + \frac{1}{2}}{\frac{Ey_0}{k} + 1} \equiv F_{cs}(E, k, y_0)$$

Then the non-zero Christoffel symbols are as follows:

$$\text{Eq 19:} \quad \left\{ \begin{matrix} 0 \\ 00 \end{matrix} \right\} = - \left[2y_0 \left(\frac{Ey_0}{k} + 1 \right) \right]^{-1}$$

$$\text{Eq 20:} \quad \left\{ \begin{matrix} 0 \\ 11 \end{matrix} \right\} = -y_0 F_{cs}(E, k, y_0)$$

$$\text{Eq 21:} \quad \left\{ \begin{matrix} 0 \\ 22 \end{matrix} \right\} = -y_0 \sin^2(y_1) F_{cs}(E, k, y_0)$$

$$\text{Eq 22:} \quad \left\{ \begin{matrix} 1 \\ 01 \end{matrix} \right\} = \frac{1}{y_0} F_{cs}(E, k, y_0)$$

$$\text{Eq 23:} \quad \left\{ \begin{matrix} 1 \\ 22 \end{matrix} \right\} = -\sin(y_1) \cos(y_1)$$

$$\text{Eq 24:} \quad \left\{ \begin{matrix} 2 \\ 02 \end{matrix} \right\} = \frac{1}{y_0} F_{cs}(E, k, y_0)$$

$$\text{Eq 25:} \quad \left\{ \begin{matrix} 2 \\ 12 \end{matrix} \right\} = \cot(y_1)$$